

Power Divider dan Coupler (2)

TTG4D3 – Rekayasa Gelombang Mikro

Oleh

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Outline

- 4 Port Coupler

4-Port Coupler

- Symmetric

$$S = \begin{bmatrix} 0 & \alpha & j\beta & 0 \\ \alpha & 0 & 0 & j\beta \\ j\beta & 0 & 0 & \alpha \\ 0 & j\beta & \alpha & 0 \end{bmatrix}$$

- Anti-Symmetric

$$S = \begin{bmatrix} 0 & \alpha & \beta & 0 \\ \alpha & 0 & 0 & -\beta \\ \beta & 0 & 0 & \alpha \\ 0 & -\beta & \alpha & 0 \end{bmatrix}$$

LOSSLESS???

Directional Coupler

$$S = \begin{bmatrix} 0 & \alpha & j\beta & 0 \\ \alpha & 0 & 0 & j\beta \\ j\beta & 0 & 0 & \alpha \\ 0 & j\beta & \alpha & 0 \end{bmatrix}$$

$$S = \begin{bmatrix} 0 & \sqrt{1-c^2} & jc & 0 \\ \sqrt{1-c^2} & 0 & 0 & jc \\ jc & 0 & 0 & \sqrt{1-c^2} \\ 0 & jc & \sqrt{1-c^2} & 0 \end{bmatrix}$$

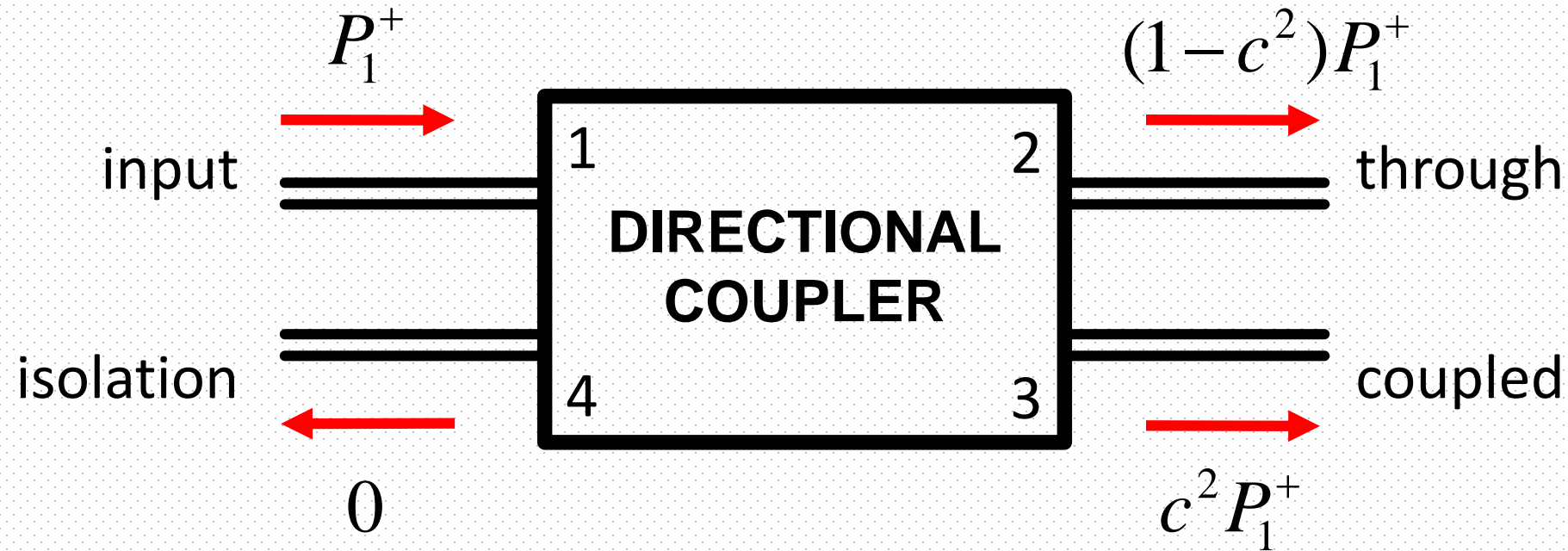
c = koefisien Coupling

$$\alpha = \sqrt{1-\beta^2}$$



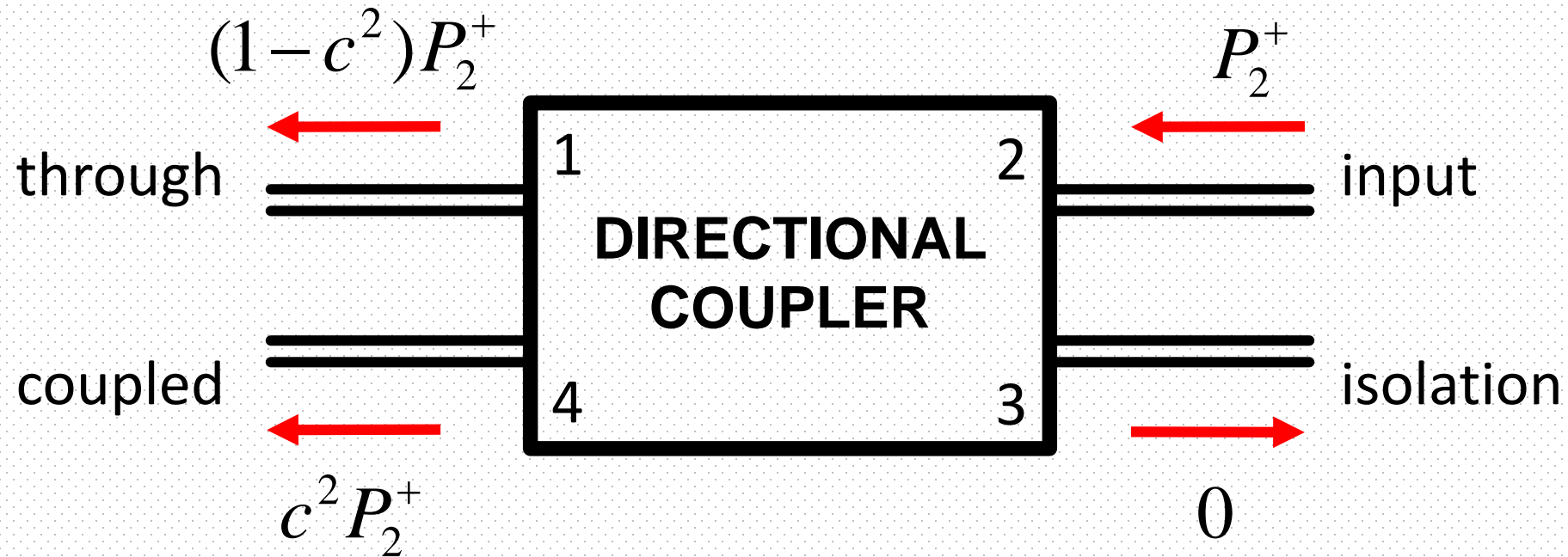
Directional Coupler (2)

Jika input pada port - 1



Directional Coupler (3)

Bagaimana Jika input pada port – 2?



Directional Coupler (4)

- Jadi..

input	through	coupled	isolation
Port-1	Port-2	Port-3	Port-4
Port-2	Port-1	Port-4	Port-3
Port-3	Port-4	Port-1	Port-2
Port-4	Port-3	Port-2	Port-1

Directional Coupler (5)

- Non-ideal Directional Coupler

$$S = \begin{bmatrix} S_{11} & S_{21} & jc & S_{41} \\ S_{21} & S_{11} & S_{411} & jc \\ jc & S_{41} & S_{11} & S_{21} \\ S_{41} & jc & S_{21} & S_{11} \end{bmatrix}$$

Directional Coupler (6)

- Coupling (C) $\rightarrow C(dB) = 10\log_{10}\left[\frac{P_1^+}{P_3^-}\right] = -10\log_{10}|jc|^2$

- Directivity (D) $\rightarrow D(dB) = 10\log_{10}\left[\frac{P_3^-}{P_4^-}\right] = 10\log_{10}\left[\frac{|jc|^2}{|S_{41}|^2}\right]$

- Isolation (I) $\rightarrow I(dB) = 10\log_{10}\left[\frac{P_1^+}{P_4^-}\right] = -10\log_{10}|S_{41}|^2 \rightarrow I(dB) = C(dB) + D(dB)$



Directional Coupler (7)

- Mainline Loss (ML) $\rightarrow ML(dB) = 10\log_{10}\left[\frac{P_1^+}{P_2^-}\right] = -10\log_{10}\left[|S_{21}|^2\right]$
- Coupling Loss (CL) $\rightarrow CL(dB) = -10\log_{10}\left[1 - |jc|^2\right]$
- Isolation (I) $\rightarrow IL(dB) = ML(dB) - CL(dB)$

Quadrature Hybrid

Simetrik

$$S = \begin{bmatrix} 0 & \alpha & \beta & 0 \\ \alpha & 0 & 0 & -\beta \\ \beta & 0 & 0 & \alpha \\ 0 & -\beta & \alpha & 0 \end{bmatrix}$$

Anti-simetrik

$$S = \begin{bmatrix} 0 & \alpha & j\beta & 0 \\ \alpha & 0 & 0 & j\beta \\ j\beta & 0 & 0 & \alpha \\ 0 & j\beta & \alpha & 0 \end{bmatrix}$$



90 Degrees Hybrid Coupler

$$S = \begin{bmatrix} 0 & \alpha & \beta & 0 \\ \alpha & 0 & 0 & -\beta \\ \beta & 0 & 0 & \alpha \\ 0 & -\beta & \alpha & 0 \end{bmatrix}$$

$$\alpha = \frac{-j}{\sqrt{2}}$$
$$j\beta = \frac{-1}{\sqrt{2}}$$

jika

maka

**Matched
Lossless
Resiprok**

$$S = \begin{bmatrix} 0 & -j/\sqrt{2} & -1/\sqrt{2} & 0 \\ -j/\sqrt{2} & 0 & 0 & -1/\sqrt{2} \\ -1/\sqrt{2} & 0 & 0 & -j/\sqrt{2} \\ 0 & -1/\sqrt{2} & -j/\sqrt{2} & 0 \end{bmatrix}$$



90 Degrees Hybrid Coupler

Contoh :

Jika daya sebesar 10mW masuk ke port 3, berapa daya yang keluar di port 1 dan port 4?

$$V_1(z, t) = \frac{|V_{03}^-|}{\sqrt{2}} \cos(\omega_0 t + \beta z)$$

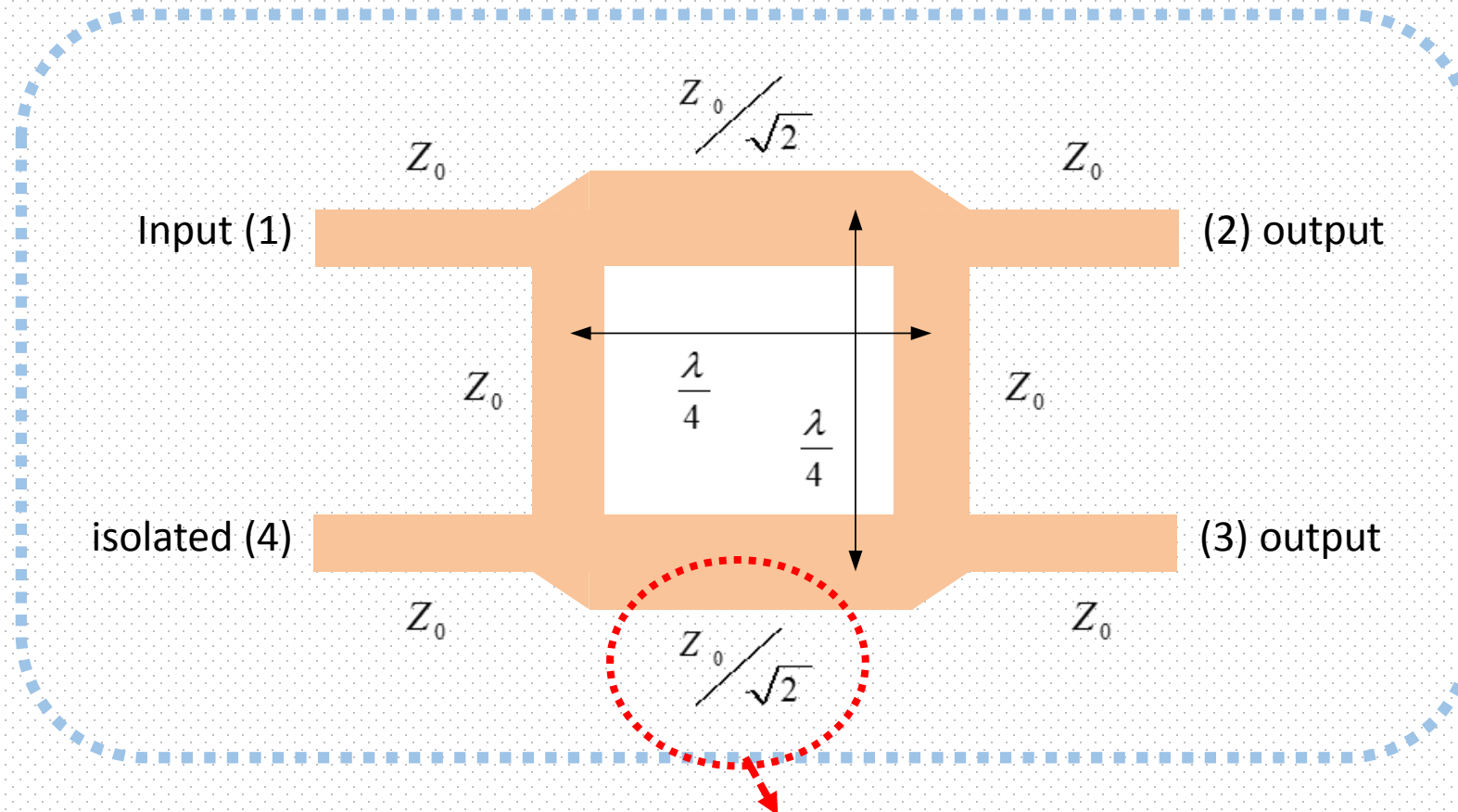
$$S = \begin{bmatrix} 0 & -j/\sqrt{2} & -1/\sqrt{2} & 0 \\ -j/\sqrt{2} & 0 & 0 & -1/\sqrt{2} \\ -1/\sqrt{2} & 0 & 0 & -j/\sqrt{2} \\ 0 & -1/\sqrt{2} & -j/\sqrt{2} & 0 \end{bmatrix}$$

$$V_4(z, t) = \frac{|V_{03}^-|}{\sqrt{2}} \sin(\omega_0 t + \beta z)$$

Magnitude pada port-1 dan port-4 sama, tetapi fasanya berbeda 90 derajat



Quadrature Coupler



Mirip dengan wilkinson power divider yang menggunakan $\lambda/4$



Coupled-Line Directional Coupler

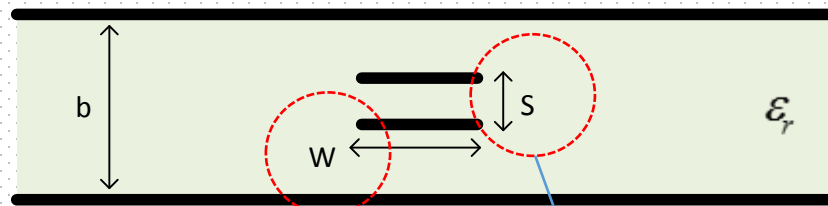
Quadrature hybrid adalah coupler 3dB, bagaimana membuat coupler dengan coupling yang lebih kecil? Seperti 10dB, 20dB atau 30dB?

Dengan menggunakan Coupled-Line!

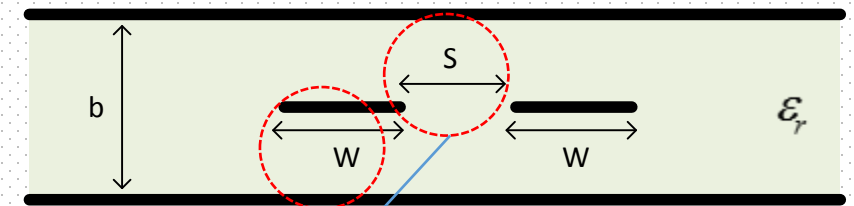


Coupled-Lines Coupler

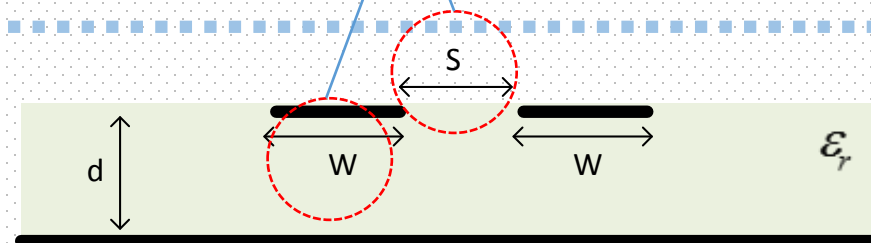
Coupled-Line - Stacked



Coupled-Line - Planar



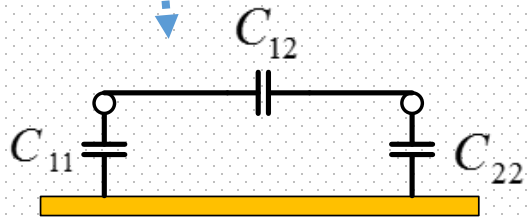
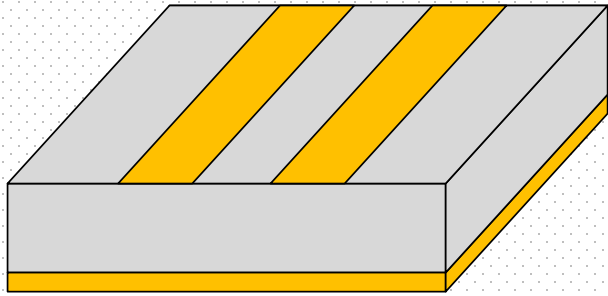
- 2 saluran transmisi yang didekatkan satu sama lain akan mengkopling daya satu sama lain
- Kedekatan ini akan memodifikasi medan elektromagnetik (juga arus dan tegangan) juga impedansi saluran



Coupled Microstrip

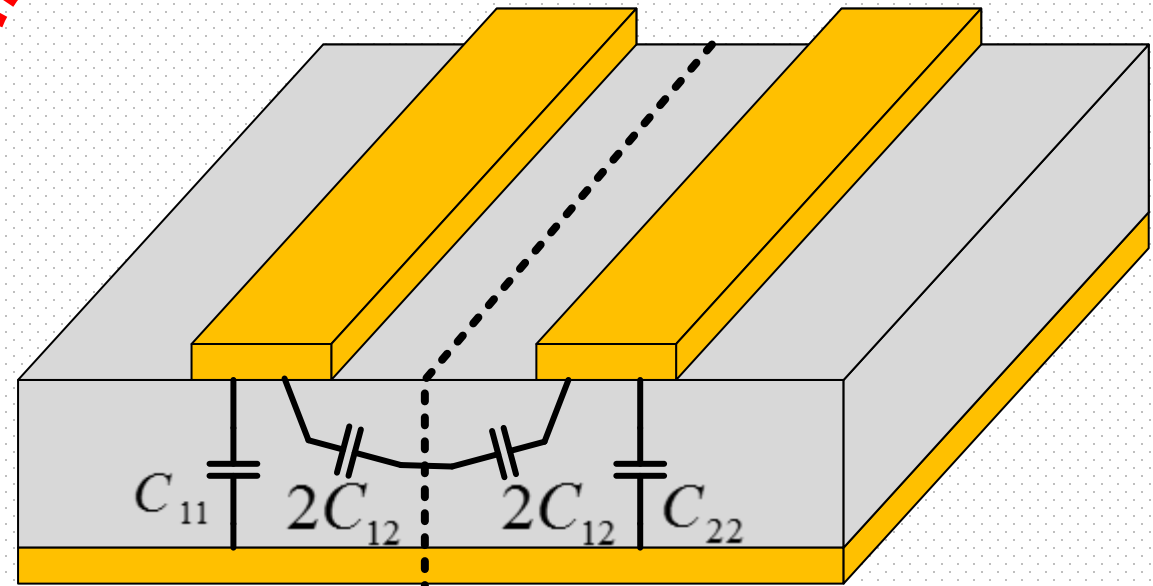


Quadrature Coupler



Jika 2 saltran identik,
maka $C_{11} = C_{22}$

Rangkaian identik, simetrik, bisa dianalisa dengan
odd/even analysis.

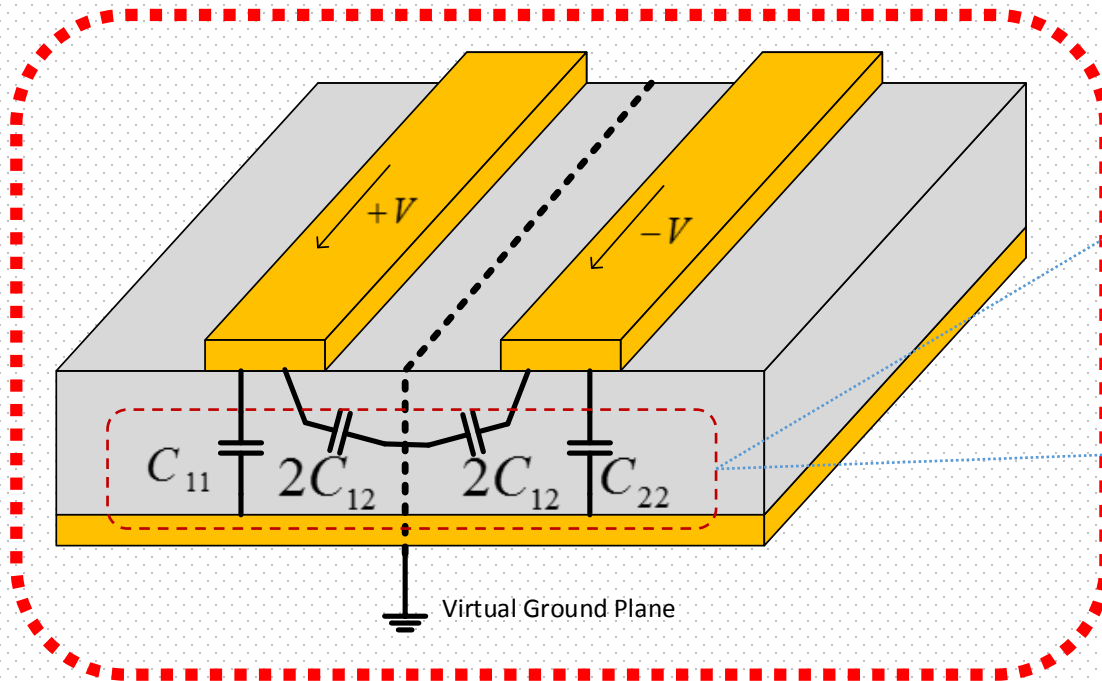


Plane of Coupler Symmetry



Quadrature Coupler

Odd Mode : Gelombang/tegangan datang sepanjang saltran berlawanan, megnitude sama, tapi fasa berbeda 180 derajat.



Kapasitansi persatuan panjang

$$C_0 = C_{11} + 2C_{12} = C_{22} + 2C_{12}$$

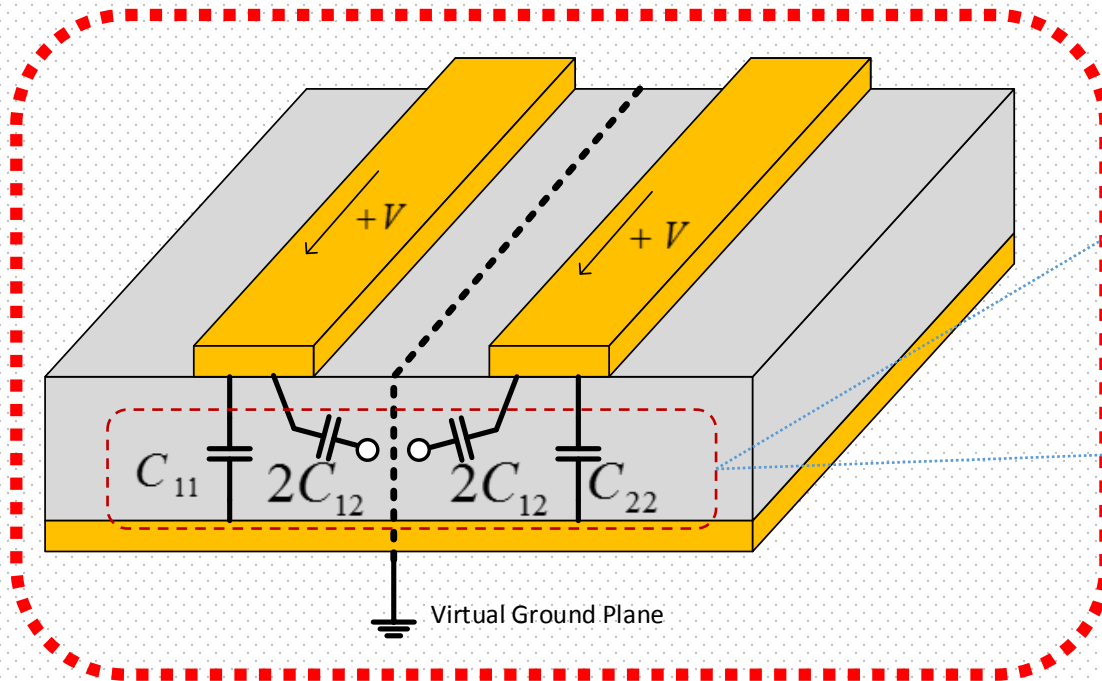
Impedansi Karakteristik

$$Z_0^o = \sqrt{\frac{L}{C_o}}$$



Quadrature Coupler

Even Mode : Gelombang/tegangan datang sepanjang saluran sebanding, magnitude dan fasa sama



Kapasitansi persatuan panjang

$$C_0 = C_{11} = C_{22}$$

Impedansi Karakteristik

$$Z_0^e = \sqrt{\frac{L}{C_e}}$$



Quadrature Coupler

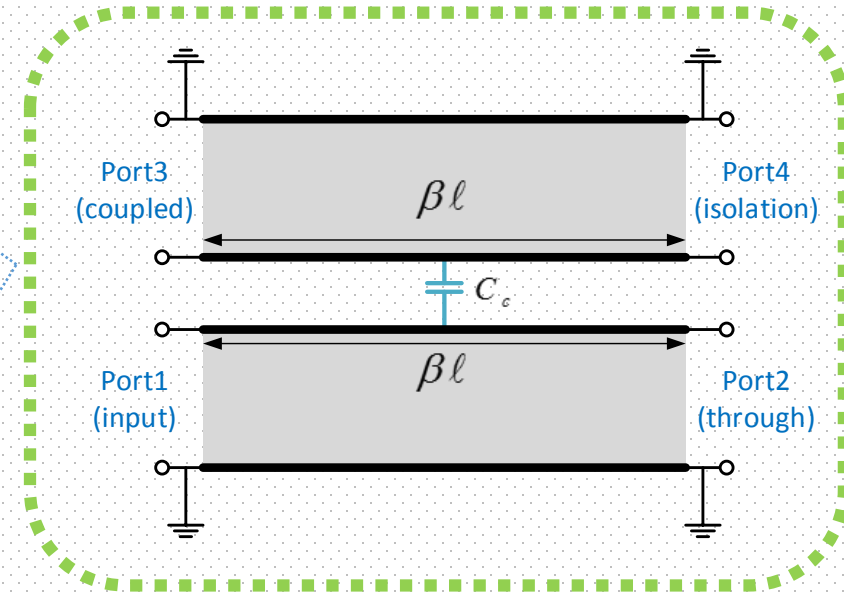
$$S = \begin{bmatrix} 0 & -j\sqrt{1-c^2} & c & 0 \\ -j\sqrt{1-c^2} & 0 & 0 & c \\ c & 0 & 0 & -j\sqrt{1-c^2} \\ 0 & c & -j\sqrt{1-c^2} & 0 \end{bmatrix}$$

$$Z_0^e = Z_0 \sqrt{\frac{1+c}{1-c}}$$

$$Z_0^o = Z_0 \sqrt{\frac{1-c}{1+c}}$$

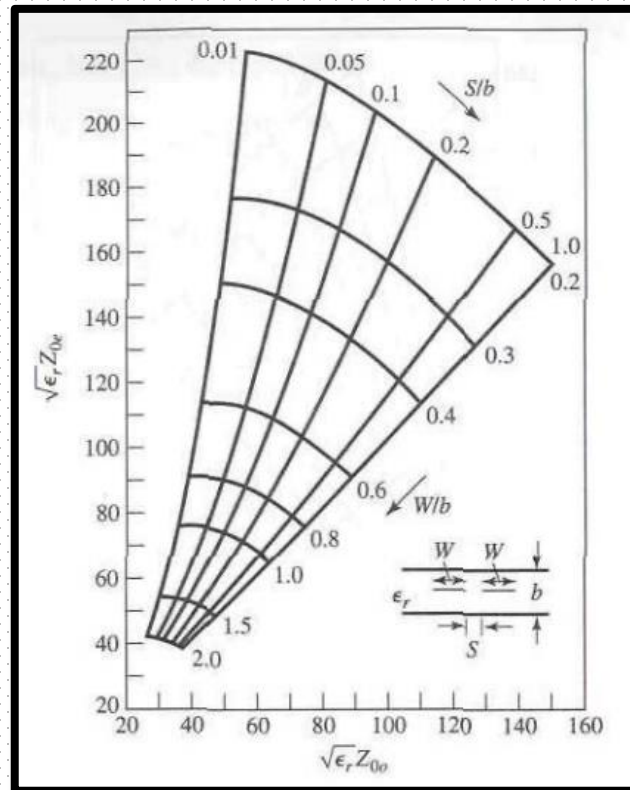
$$Z_0^e Z_0^o = Z_0$$

$$c = \frac{Z_0^e - Z_0^o}{Z_0^e + Z_0^o}$$

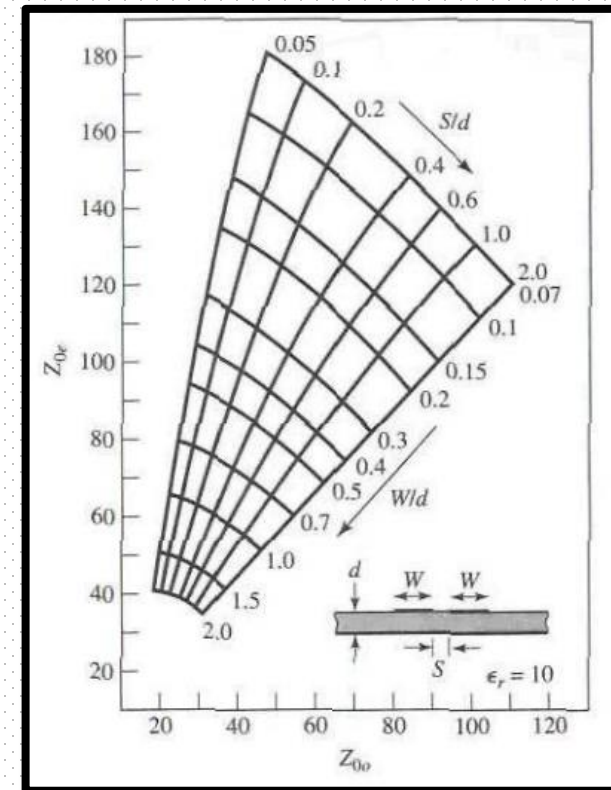


Quadrature Coupler

Edge-Coupled Striplines



Coupled Microstrip Lines



Contoh : Single Section Coupler Design

Design a 20 dB single section coupled line coupler in stripline with a 0,158 cm ground plane spacing, dielectric constant of 2,56. a characteristic impedance of 50 ohm and center frequency of 3 GHz.



Penyelesaian - Quadrature Coupler

1

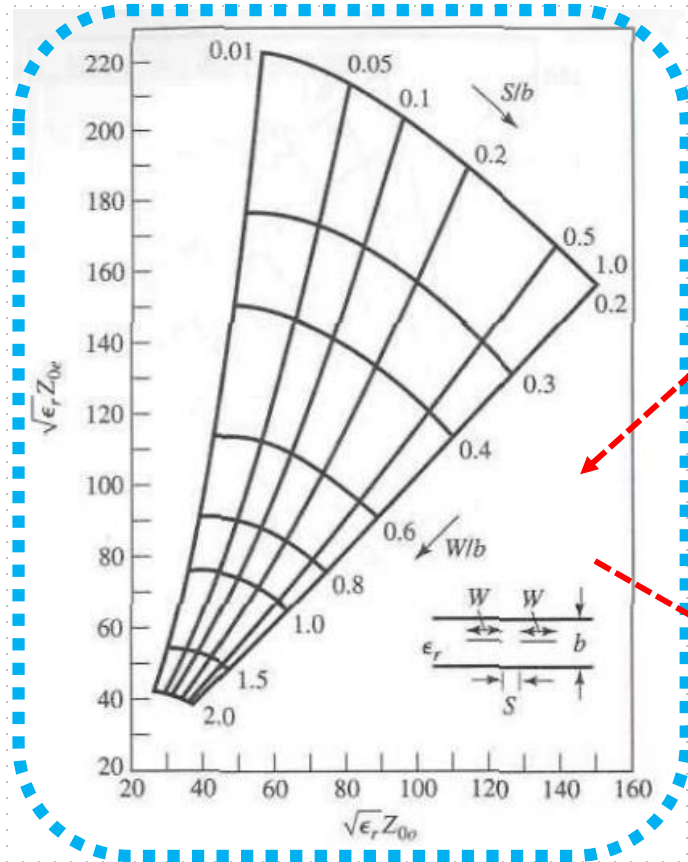
Cari coupling vector!

$$C = 10^{-20/20} = 0,1$$

Cari Z_0 even/odd

$$Z_{0e} = 50 \sqrt{\frac{1,1}{0,9}} = 55,28\Omega$$

$$Z_{0o} = 50 \sqrt{\frac{0,9}{1,1}} = 45,23\Omega$$



Gunakan grafik

$$\sqrt{\epsilon_r} Z_{0e} = 88,4$$

$$\sqrt{\epsilon_r} Z_{0o} = 72,4$$

$$W/b = 0,72$$

$$S/b = 0,34$$

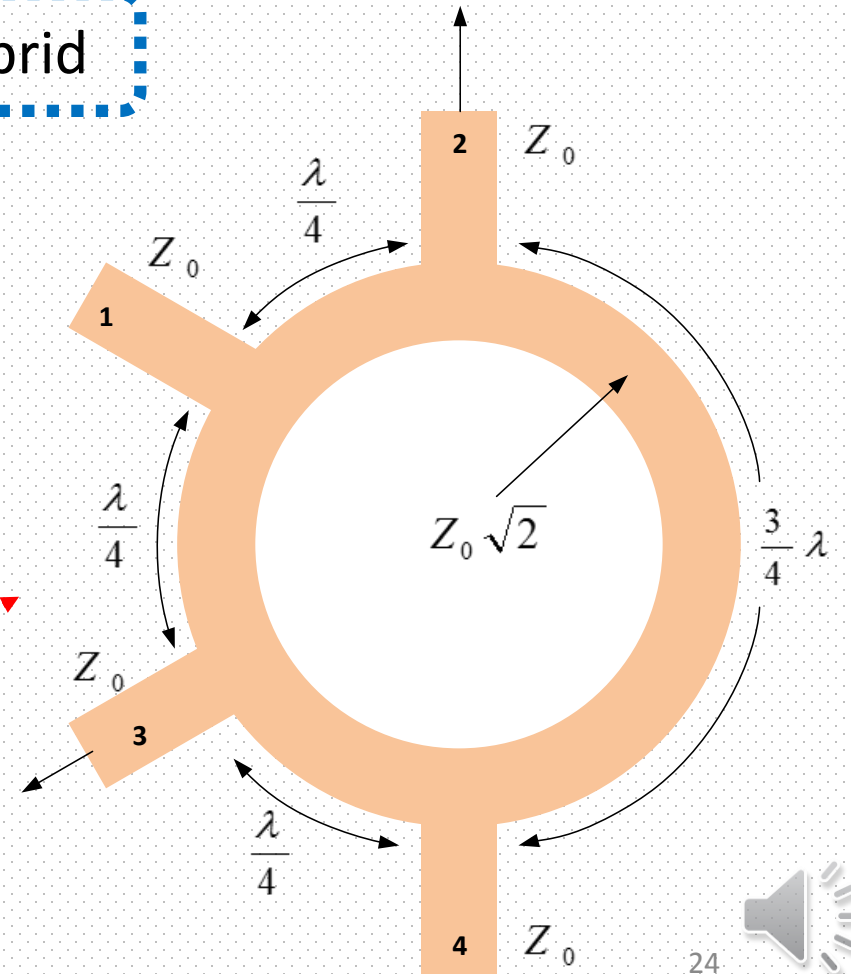
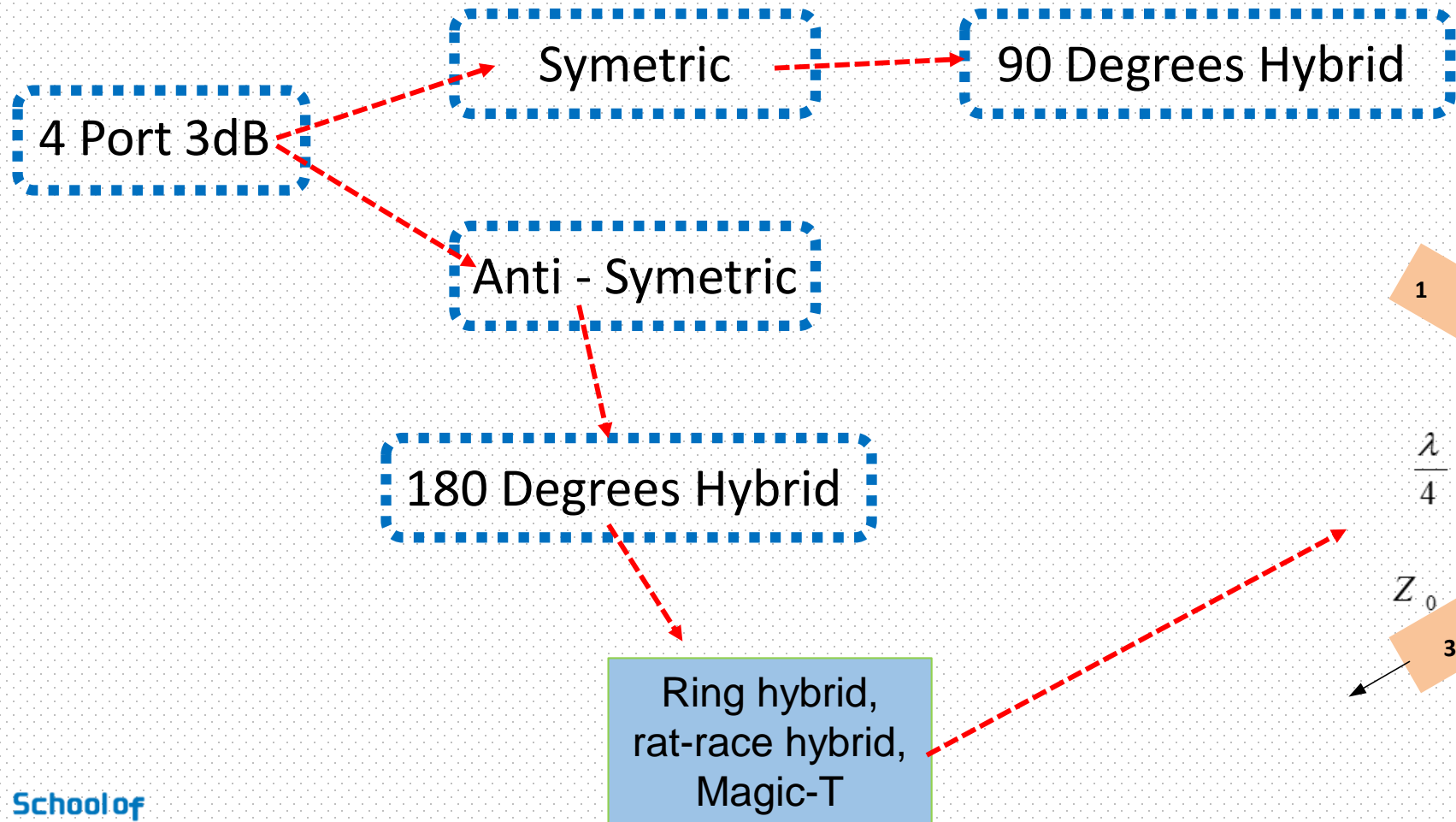
$$W = 0,72b$$

$$= 0,114\text{cm}$$

$$S = 0,34b$$

$$= 0,054\text{cm}$$

180 Degrees Coupler



Contoh : Single Section Coupler Design

$$S = \begin{bmatrix} 0 & \alpha & \beta & 0 \\ \alpha & 0 & 0 & -\beta \\ \beta & 0 & 0 & \alpha \\ 0 & -\beta & \alpha & 0 \end{bmatrix}$$

**Matched
Lossless
Resiprok**

$$S = \begin{bmatrix} 0 & 1/\sqrt{2} & 1/\sqrt{2} & 0 \\ 1/\sqrt{2} & 0 & 0 & -1/\sqrt{2} \\ 1/\sqrt{2} & 0 & 0 & 1/\sqrt{2} \\ 0 & -1/\sqrt{2} & 1/\sqrt{2} & 0 \end{bmatrix}$$



Referensi

- Microwave Engineering 3rd Edition, David M. Pozar

Terima Kasih